

## REPORT DOCUMENTATION PAGE

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OMB No. 0704-0188

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1. AGENCY USE ONLY (Leave blank)		2. REPORT DATE March 12, 1990		3. REPORT TYPE AND DATES COVERED Technical	
4. TITLE AND SUBTITLE  Computer Program for Mode Search in Partially-filled Waveguide				5. FUNDING NUMBERS  DAAL03-87-K-0088	
6. AUTHOR(S)  T. E. van Deventer, P. B. Katehi					
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)  University of Michigan Ann Arbor, MI 48109				8. PERFORMING ORGANIZATION REPORT NUMBER	
9. SPONSORING / MONITORING AGENCY NAME(S) AND ADDRESS(ES)  U. S. Army Research Office P. O. Box 12211 Research Triangle Park, NC 27709-2211				10. SPONSORING / MONITORING AGENCY REPORT NUMBER  ARO 23836.14-EL	
11. SUPPLEMENTARY NOTES The view, opinions and/or findings contained in this report are those of the author(s) and should not be construed as an official Department of the Army position, policy, or decision, unless so designated by other documentation.					
12a. DISTRIBUTION / AVAILABILITY STATEMENT  Approved for public release; distribution unlimited.				12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words)  The FORTRAN program PFW.FTN (Partially-Filled Waveguide) was written to compute the complex propagation constant of the hybrid modes propagating in an inhomogeneously-filled waveguide with any number of lossy substrates and non-perfectly conducting walls.					
14. SUBJECT TERMS  Computer Programs, Mode Search, Waveguides, Fortran				15. NUMBER OF PAGES 9	
				16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT UNCLASSIFIED	18. SECURITY CLASSIFICATION OF THIS PAGE UNCLASSIFIED	19. SECURITY CLASSIFICATION OF ABSTRACT UNCLASSIFIED	20. LIMITATION OF ABSTRACT UL		

AD-A225 943

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# Computer Program for Mode Search in Partially-filled Waveguide

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Ann Arbor, MI 48109

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Accession for	
DTIC	<input checked="" type="checkbox"/>
DDIC	<input type="checkbox"/>
Unpublished	<input type="checkbox"/>
Distribution	
For	
Distribution/	
Availability Codes	
and/or	
Special	
A-1	

This work was supported by the Army Research Office under contract project  
DAAL03-K-0088 (23836-EL).



90 08 28 050

# Computer Program for Mode Search in Partially-filled Waveguide

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Ann Arbor, MI

## GOAL

The FORTRAN program PFW.FTN (Partially-Filled Waveguide) was written to compute the complex propagation constant of the hybrid modes propagating in an inhomogeneously-filled waveguide with any number of lossy substrates and non-perfectly conducting walls.

## FORMULATION

The general version of the program solves for the hybrid TE and TM to x modes that propagate in structures as shown in Figure 1. To determine the possible propagation constants  $k_z$ , the following transcendental equations corresponding to these hybrid modes are solved for *LSM* ( $TM_x$ ) modes as

$$\frac{k_{x1}}{\epsilon_1} \tan k_{x1} h_1 = -\frac{k_{x2}}{\epsilon_2} \tan k_{x2} h_2 \quad (1)$$

and for *LSE* ( $TE_x$ ) modes

$$\frac{k_{x1}}{\mu_1} \cot k_{x1} h_1 = -\frac{k_{x2}}{\mu_2} \cot k_{x2} h_2 \quad (2)$$

with

$$k_{x1}^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 = \omega^2 \epsilon_1 \mu_1 \quad (3)$$

$$k_{x2}^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 = \omega^2 \epsilon_2 \mu_2. \quad (4)$$

The hybrid modes are denoted  $LSE_{mn}$  and  $LSM_{mn}$ . The transcendental equations have an infinite number of solutions for a given mode number  $n$ . The index  $m$  denotes the order of these solutions. For  $b > a$ , the dominant mode is the  $LSM_{01}$  mode ( $m = 0, n = 1$ ) followed by  $m = 1$ , and so on. For  $b < a$ , the first mode is an  $LSE$  mode with  $n = 0$ . In this case the numbering on the index  $m$  starts at  $m = 1$ , then  $m = 2$ , and so on. The numbering is chosen to be consistent with that of the empty waveguide [1].

The equations (1), (2) are derived using the transverse resonance method, since the structure at resonance reduces to a transmission-line structure with propagation in the  $x$ -direction. In the case of perfectly conducting walls, the end transmission-lines are shortcircuited as shown in Figure 2. However finite conductivity of the metal housing has been implemented in the PFW.FTN where the top and bottom walls can have a conductivity  $\sigma$ , which in turns can be described by a load at the end of the transmission line. The program also accounts for substrate losses with the option of inputting the dielectric and magnetic loss tangents.

$$\epsilon_i = \epsilon_{ri} (1 - j \tan \delta_i) \quad (5)$$

$$\mu_i = \mu_{ri} (1 - j \tan \gamma_i). \quad (6)$$

This program allows to compute the complex propagation constant of any propagating mode in a rectangular waveguide structure, as a function of frequency. It can also calculate the cut-off frequency of the modes by choosing a frequency increment small enough around  $k_z = 0$ .

## DESCRIPTION

The geometry of the structure is inputted through a user-friendly menu program. The output is written in a file and on the screen,

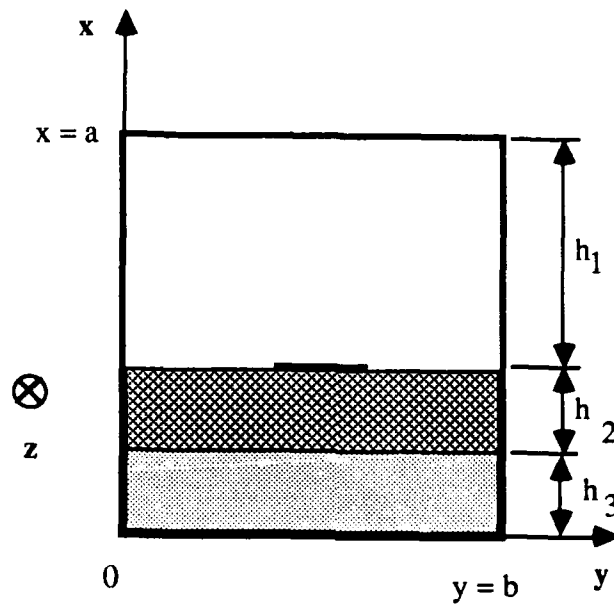


Figure 1: Partially-filled waveguide configuration

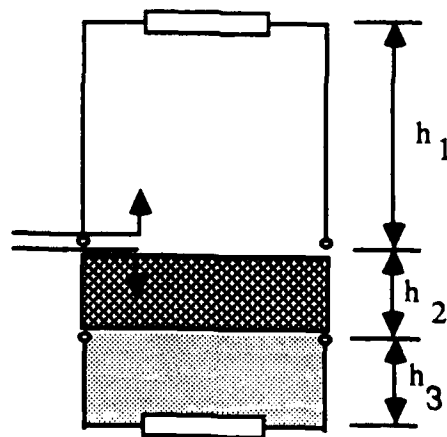


Figure 2: Transmission-line Analogy

and gives the propagation constant of the modes propagating within the frequency range of interest.

### **.1 menu**

The menu is an interactive program that allows for on-screen creation of the input data file. Also changes can be made on the screen by entering the variable name to be changed (e.g. FSTR to change the starting frequency). The program will then prompt for a new value of the variable. Dimensions can be entered either in centimeters or inches. Conductor losses in the top and bottom walls may be included, in which case the conductivity of the walls should be given. The maximum mode number  $n$  refers to the discussion in the previous section. The output is written in a file called 'RESULT'.

### **.2 program**

The PFW.FTN program calculates the roots of (1) and (2) for the lossless case. When losses are considered, the roots of the transcendental equations are found using Muller's method with deflation. The present program calls for the following subroutines of the *IMSL* library (November 1, 1984 release) [2]

- ZANLYT ( find the zeros of a univariate complex function using Muller's method)
- UGETIO
- USPKD
- UERTST.

These subroutines have to be bound to the main program PFW.FTN for the program to run. If this library is not available, a lossless version of the program may be requested.

### **.3 limitations**

The program PFW.FTN is a generalized code that can handle any number of dielectric layers. However, for programming purposes, the arrays have been dimensioned to a maximum of 20 layers.

## VERIFICATION

Using the approach described in the previous section a computer program was developed to calculate the complex propagation constant. The validity of this program has been verified in the case of lossless substrates. Good agreement with Yamashita's paper [3] is shown, and the results of the program PFW.FTN given in the next section may be compared to Figure 3.

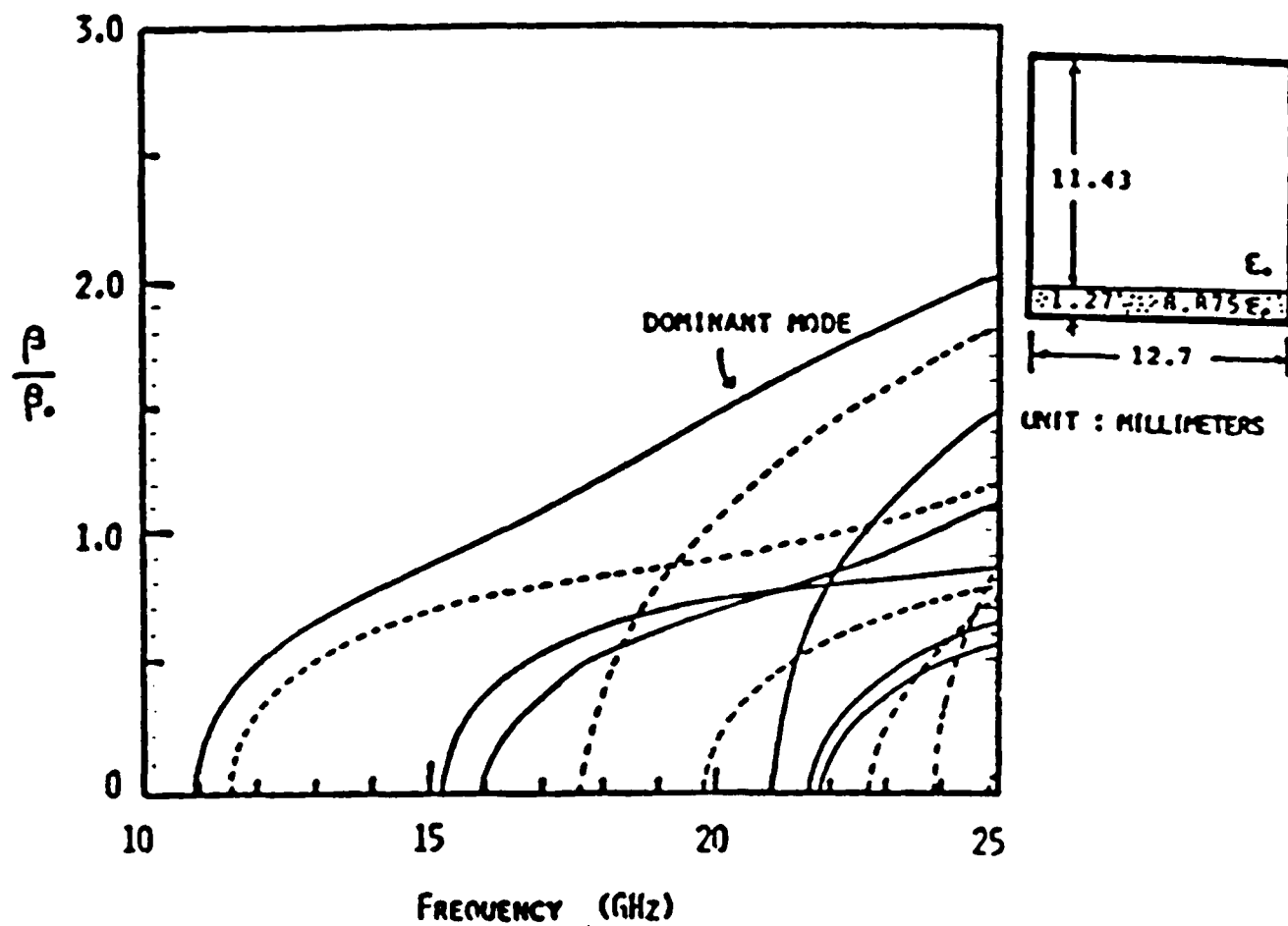


Figure 3: Propagation Constant as a function of frequency (comparison with Yamashita)



## I/O FILES AND CODE

.1 screen sample

S p

THE UNIVERSITY OF MICHIGAN COLLEGE OF ENGINEERING  
RADIATION LABORATORY  
ANN ARBOR, MICHIGAN

```

*****
MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM
MM M  M MM  MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM
MM M M MM  MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM
MM M M MM  MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM
MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM MM
MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM
*****

```

THIS PROGRAM CALCULATES THE PROPAGATION CONSTANT OF THE HYBRID MODES  
EXCITED IN PARTIALLY-FILLED WAVEGUIDES

T. EMILIE VAN DEVENTER -- AND -- LINDA P. B. KATEHI

MARCH 11, 1990 VERSION

Fortran PAUSE

Type return to continue

Enter name of configuration data file;

yamashita

ENTER START FREQUENCY (GHz) :

10

ENTER STOP FREQUENCY (GHz) :

25

ENTER INCREMENT FREQUENCY (GHz):

1

Select units:

[1] inches

[2] centimeters

2

Enter # OF LAYERS IN WAVEGUIDE:

2

Enter permittivity for layer 1

1

Enter permittivity loss tangent for layer 1

0

Enter permeability for layer 1

1

Enter permeability loss tangent for layer 1

0

Enter height of layer 1

1.143

Enter permittivity for layer 2

8.875

Enter permittivity loss tangent for layer 2

0

Enter permeability for layer 2

1

Enter permeability loss tangent for layer 2

0

Enter height of layer 2

.127

Enter waveguide dimension along x:

1.27

Enter waveguide dimension along y:

1.27

Enter maximum # of modes to find

3

DIMENSIONS ARE TO BE ENTERED IN CENTIMETERS

Name of geometry configuration file (NAME) yamashita

the units are CM

cavity dimension along x [A] : 1.2700000

cavity dimension along y [B] : 1.2700000

START FREQUENCY TO RUN (GHz) [FSTR]: 10.00000

STOP FREQUENCY TO RUN (GHz) [FSTP]: 25.00000

INCREMENT FREQUENCY (GHz) [FNCR]: 1.000000

NUMBER OF DIELECTRIC LAYERS (NLY) : 2

RELATIVE ELECTRIC PARAMETERS OF LAYERS:

	dielectric constant	loss tangent	real permeability	imaginary permeability
Layer 1	[EL1R] : 1.000000	[EL1I] : 0.000000	[EL1M] : 1.000000	[M1M] : 0.000000
Layer 2	[EL2R] : 8.875000	[EL2I] : 0.000000	[EL2M] : 1.000000	[M2M] : 0.000000

GEOMETRY OF DIELECTRIC LAYERS:

	CM
Layer 1 thickness:	[L1B] : 1.143000
Layer 2 thickness:	[L2B] : 0.127000

PROGRAM PARAMETERS

max. n mode number

[M] 3

## CONDUCTOR LOSSES

Include lower ground losses : [GL] F  
 Include upper ground losses : [UL] F  
 Conductivity of the walls : [SIG] 0.00000000E+00

Enter Variable Name [\*\*] or <return>

operating frequency	mode excited	kz	propagation kz/k0	constant alpha (Np/m)
11.00000	LSM 0 1	31.31126	0.13591	0.00000
12.00000	LSE 1 0	79.74963	0.31731	0.00000
12.00000	LSM 0 1	120.35992	0.47890	0.00000
13.00000	LSE 1 0	135.77371	0.49867	0.00000
13.00000	LSM 0 1	174.46198	0.64077	0.00000
14.00000	LSE 1 0	177.91298	0.60677	0.00000
14.00000	LSM 0 1	223.21684	0.76127	0.00000
15.00000	LSE 1 0	214.72264	0.68348	0.00000
15.00000	LSM 0 1	272.61243	0.86775	0.00000
16.00000	LSE 1 0	248.85355	0.74262	0.00000
16.00000	LSE 1 1	27.13669	0.08098	0.00000
16.00000	LSM 0 1	326.30457	0.97374	0.00000
16.00000	LSM 1 1	126.81892	0.37845	0.00000
16.99999	LSE 1 0	281.65442	0.79106	0.00000
16.99999	LSE 1 1	134.67567	0.37825	0.00000
16.99999	LSM 0 1	386.91238	1.08669	0.00000
16.99999	LSM 1 1	188.03099	0.52811	0.00000
17.99999	LSE 1 0	314.07828	0.83312	0.00000
17.99999	LSE 1 1	193.52902	0.51335	0.00000
17.99999	LSM 0 1	455.72186	1.20884	0.00000
17.99999	LSM 1 1	233.84915	0.62030	0.00000
17.99999	LSM 0 2	155.26567	0.41186	0.00000
18.99999	LSE 1 0	347.03436	0.87209	0.00000
18.99999	LSE 1 1	243.39511	0.61165	0.00000
18.99999	LSM 0 1	532.32367	1.33772	0.00000
18.99999	LSM 1 1	272.13550	0.68387	0.00000
18.99999	LSM 0 2	315.90094	0.79385	0.00000
19.99999	LSE 1 0	381.62134	0.91105	0.00000
19.99999	LSE 2 0	87.68021	0.20932	0.00000
19.99999	LSE 1 1	290.59106	0.69374	0.00000
19.99999	LSM 0 1	614.82782	1.46779	0.00000
19.99999	LSM 1 1	305.95987	0.73043	0.00000
19.99999	LSM 0 2	440.95157	1.05269	0.00000
20.99999	LSE 1 0	419.31534	0.95337	0.00000
20.99999	LSE 2 0	200.72998	0.45639	0.00000
20.99999	LSE 1 1	338.57596	0.76980	0.00000
20.99999	LSM 0 1	700.75470	1.59327	0.00000
20.99999	LSM 0 2	554.51080	1.26076	0.00000
20.99999	LSM 0 3	39.09147	0.08888	0.00000
21.99999	LSE 1 0	461.96701	1.00260	0.00000
21.99999	LSE 2 0	272.47369	0.59135	0.00000
21.99999	LSE 1 1	390.15616	0.84675	0.00000
21.99999	LSE 2 1	114.23763	0.24793	0.00000
21.99999	LSM 0 1	787.95502	1.71010	0.00000
21.99999	LSM 1 1	365.93430	0.79419	0.00000
21.99999	LSM 2 1	71.16162	0.15444	0.00000
21.99999	LSM 0 2	661.28510	1.43518	0.00000
21.99999	LSM 0 3	362.40820	0.78653	0.00000
22.99999	LSE 1 0	511.25302	1.06133	0.00000
22.99999	LSE 2 0	328.50262	0.68195	0.00000
22.99999	LSE 1 1	447.42371	0.92882	0.00000
22.99999	LSE 2 1	216.15340	0.44872	0.00000
22.99999	LSE 1 2	128.89127	0.26757	0.00000
22.99999	LSM 0 1	874.98932	1.81642	0.00000
22.99999	LSM 1 1	393.56696	0.81702	0.00000
22.99999	LSM 2 1	180.87822	0.37549	0.00000
22.99999	LSM 0 2	762.90967	1.58375	0.00000
22.99999	LSM 0 3	525.42639	1.09075	0.00000
23.99999	LSE 1 0	567.67902	1.12936	0.00000
23.99999	LSE 2 0	374.12955	0.74431	0.00000
23.99999	LSE 1 1	510.94788	1.01650	0.00000
23.99999	LSE 2 1	280.68002	0.55840	0.00000
23.99999	LSE 1 2	278.37512	0.55381	0.00000
23.99999	LSM 0 1	961.05621	1.91196	0.00000
23.99999	LSM 1 1	420.13651	0.83584	1.78549
23.99999	LSM 2 1	244.50510	0.48643	0.00000
23.99999	LSM 0 2	860.26398	1.71144	0.00000
23.99999	LSM 0 3	658.85938	1.31076	0.00000
24.99999	LSE 1 0	630.29608	1.20378	0.00000
24.99999	LSE 2 0	412.43860	0.78770	0.00000
24.99999	LSE 1 1	579.72522	1.10719	0.00000
24.99999	LSE 2 1	330.02109	0.63029	0.00000
24.99999	LSE 1 2	390.52069	0.74584	0.00000
24.99999	LSM 0 1	1045.78235	1.99730	0.00000
24.99999	LSM 1 1	446.21091	0.85220	1.10039
24.99999	LSM 2 1	294.31281	0.56210	0.00000
24.99999	LSM 0 2	953.98407	1.82198	0.00000
24.99999	LSM 1 2	124.01501	0.23685	0.00000
24.99999	LSM 0 3	777.25629	1.48445	0.00000

Fortran STOP

## .2 FORTRAN code

```

c*****
c
c      t.e. van deventer
c      radiation laboratory
c      room 3121, eecs bldg
c      (313) 769-2975
c      department of electrical engineering and computer science
c      the university of michigan
c      ann arbor, mi 48105
c
c*****
c
c      program pfw.ftn
c
c      this program is divided into 3 parts,
c      (1) main program
c      (2) subroutines
c      (3) functions
c
c      date :   o  31 may 1989
c
c      bind pfw.bin  muller.bin -b p
c
c      topic :
c      computes the propagation constant of the lse and lsm modes
c      to solve for the transcendental equations of a general
c      n-layers inhomogeneously-filled waveguide
c
c*****
c-----
c      define parameters
c-----
      integer q,infer(1),n,nguess,nsig,kn,ms,ligne,n1
      integer itmax,ier,i,l,ifile,lunit,if,mflag
      integer groundup,groundlow,miter
      integer le,m,rdim,mid,r,mdim,index,m1,index1

      real a,b,h(20),sig,ermax,mrmax,unit
      real mu0,eps0,pi,omega,kzr,rs(0:20),rs0(0:20),is(0:20)
      real fop,fopstop,incrfr,fopn
      real epsr(20),mur(20)
      real loss_tan(20),mu_tan(20)
      real old_losstan(20),old_mutan(20)
      real incrhz
      real rwi,iwi,old_incrhz,eps,rhz,fop_1
      real attdbm,old_kzstop,as,old_incrfr
      real absdet,absdet1,amp,differ

      complex sum,sum_1,fsum
      complex kz,kz_1,j,k0,kzno loss
      complex xx(1),zs,kzstart,old_sum,eqn_c
      complex er_c(20),mur_c(20)

      character*50 config_file
      character*2 hmode

      LOGICAL do_gcl,do_ucl
c-----

```

```
c      common blocks
c-----
      common/constant/mu0,eps0,pi,omega,j,k0
      common/mike/er_c,mur_c
      common/geometry/zs,groundup,groundlow
      common/trick/fsum
      common/dimensions/mid
      common/param/mdim,le
      common/geom/a,b
      common/freq/fop,fopstop,incrfr
      common/layers/rdim,h,eps,mur,loss_tan,mu_tan
      common/operate/do_gcl,do_ucl,sig
      common/mode/m
      common/units/lunit,unit

      external eqn_c
c-----
c      read in input file
c
c      a is the x-direction (or vertical)
c      b is the y-direction (or horizontal)
c      h is the height of the layers
c      fop is the frequency of interest
c      fopstop is the maximum frequency of interest
c      incrfr is the increment of the frequency
c      groundup is a flag ( 1 = losses in upper wall considered, 0 = no conductor losses )
c      groundlow is a flag ( 1 = losses in lower wall considered, 0 = no conductor losses )
c      incrhz is the increment of the propagation constant kz
c      kzstop is an upper limit to the value of the propagation constant
c      if le is 1, calculate the lse propagation constant
c      if le is 2, calculate the lsm propagation constant
c
c-----
      call logo
      call menuc
c-----
c      open database
c-----
      open(unit=12, file='result',status='unknown')
      call writeout(12)
c-----
      groundup = 0
      groundlow = 0
      if (do_ucl) then
        groundup = 1
      endif
      if (do_gcl) then
        groundlow = 1
      endif
c-----
c      change values to SI units
c-----
      fop = fop * 1e9
      fopstop = fopstop * 1e9
      incrfr = incrfr * 1e9

      if (lunit .eq. 1) then
```

```

        unit = .0254
    else if (lunit .eq. 2) then
        unit = 1e-2
    endif

    a = a * unit
    b = b * unit
    do 103 r=1,rdim
        h(r) = h(r) * unit
    103 enddo

c-----
c   compute some constants
c-----
    pi = 4. * atan(1.)
    mu0 = 4.e-7 * pi
    eps0 = 1e-9 / (36.*pi)
    j = cmplx(0.,1.)
    mid = nint(rdim / 2.)

    mrmax = 0.0
    ermax = 0.0

    do 101 r=1,rdim
        er_c(r) = epsr(r)*cmplx(1.00,- loss_tan(r))
        mur_c(r) = mur(r)*cmplx(1.00,- mu_tan(r))
        mrmax = amax1(mur(r),mrmax)
        ermax = amax1(epsr(r),ermax)
    101 continue

    ligne = 0
    fop = fop - incrfp
    write (12,*) 'operating          mode          propag',
& 'ation constant '
    write (12,*) 'frequency          excited          kz          kz/k0'
& ', ' alpha (Np/m)'
    write (12,*) '-----'
& ', '-----'
    write (*,*) 'operating          mode          propag',
& 'ation constant '
    write (*,*) 'frequency          excited          kz          kz/k0'
& ', ' alpha (Np/m)'
    write (*,*) '-----'
& ', '-----'

c-----
c   frequency loop
c-----
    10 do 5 if=1,1000

        fop = fop + incrfp

        if (fop .gt. fopstop) then
            goto 5000
        endif
        fopn = fop * 1e-9

        omega = 2. * pi * fop

```

```
k0 = cmplx(omega * sqrt(mu0 * eps0),0.)
kz = cmplx(.01,0.) * k0
incrhz = .001 * k0
miter = 10000 * (sqrt(ermax*mrmax)+.2)
```

```
if (do_ucl .or. do_gcl) then
  amp = sqrt(pi*fop*mu0/sig)
else
  amp = 0.0
endif
zs = cmplx(amp,amp)
```

```
kzstart = kz
old_incrhz = incrhz
```

```
c-----
c   LSE / LSM loop
c-----
```

```
do 6 le=1,2

  if (le .eq. 1) then
    hmode = 'E'
  else if (le .eq. 2) then
    hmode = 'M'
  endif
```

```
  if (le .eq. 1) then
    m1 = 0
    n1 = 1
  else
    m1 = 1
    n1 = 0
  endif
```

```
c-----
c   m - mode loop
c-----
```

```
do 7 m=m1,mdim

  index1 = n1 - 1
  kz = kzstart
```

```
17      continue
```

```
      incrhz = old_incrhz
      kz_1 = cmplx(0.0,0.0)
      sum_1 = cmplx(0.0,0.0)
      mflag = 0
```

```
c-----
c   loop to compute the kz root for lossless case
c-----
```

```
12      do 20 ms=1,miter
```

```
        kz = kz + incrhz
        rkz = real(kz) / real(k0)
```

```
        if (rkz .gt. sqrt(ermax*mrmax)+.2) then
          write (*,*) 'beta > quasi-static value'
```

```
c
```



```

        goto 1000
    endif

    sum = cmplx(0.,0.)
    call hybrid(kz,sum)

c          write (*,*) 'fop,m,lekz,rkz,sum',fopn,m,le,kz,rkz,sum

c-----refinement loop-----
c
c          the loop will be used if at least one of the real or imaginary parts
c          of the sum changed sign since the previous case
c-----
        if ((real(sum_1) .lt. 0.0 .and. real(sum) .ge. 0.0)
&          .or. (real(sum_1) .gt. 0.0 .and. real(sum) .le. 0.0)
&          .or. (aimag(sum).gt.0.0 .and. aimag(sum_1).lt.0.0)
&          .or. (aimag(sum).lt.0.0 .and. aimag(sum_1).gt.0.0))
&          then

            mflag = mflag + 1
            incrkz = incrkz * 0.1
            kz = kz_1

c-----
c          check if the change of sign is due to a singularity in
c          the function (mflag test) or a root (differ)
c-----
            absdet = sqrt(real(sum)**2 + aimag(sum)**2)
            absdet1 = sqrt(real(sum_1)**2 + aimag(sum_1)**2)
            differ = abs(absdet - absdet1)

            if (differ .lt. 10.) then
                goto 13
            endif
            if (mflag .gt. 4) then
                goto 17
            endif

            goto 12
        endif

27      sum_1 = sum
        kz_1 = kz

20      continue
13      continue
        kznoloss = kz
        index1 = index1 + 1
        rs(index1) = real(kz)
        rs0(index1) = rkz
        is(index1) = 0.0

c-----
c  loop to compute the kz root for lossy case
c-----initial guess-----

40      rwi = real(kz)
        iwi = 0.0
        xx(1) = cmplx(rwi,iwi)

```

c-----muller's method (determinant)-----

```

50      continue

      eps = 1e-3
      nsig = 3
      kn = 0
      nguess = 1
      n = 1
      itmax = 100

      call zanlyt(eqn_c,eps,nsig,kn,nguess,n,xx,itmax,infer
&      ,ier)

      attdbm = - aimag(xx(1)) * 8.686

      rs(index1) = real(xx(1))
      rs0(index1) = real(xx(1)) / real(k0)
      is(index1) = attdbm

      kz = kzno loss
      goto 17

1000    continue

      do 153 ii=n1,index1
        i = index1+n1-ii
        ligne = 1
        write (*,655) fopn,hmode,ii,m,rs(i),rs0(i),is(i)
        write (12,655) fopn,hmode,ii,m,rs(i),rs0(i),is(i)
655      format(f10.5,7x,'LS',A1,'_',i2,i2,6x,f12.5,f12.5,f12.5)
        rs(i) = 0.0
        rs0(i) = 0.0
        is(i) = 0.0
153      enddo

7       continue
6       continue
      if (ligne .eq. 1) then
        write (12,*) '-----'
        write (*,*) '-----'
      endif
      ligne = 0
5       continue

5000    continue
      stop
      end

```

```
C#####
C                                     subroutines
C#####
```

```
subroutine hybrid(kz,sum)
```

-----

```
c computes the arrays corresponding to lse and lsm common terms
```

c      le = (1) corresponds to lse modes (electric)

```

c      le = (2) corresponds to lsm modes (electric)
c
c      -----cannot have eps or mu equal to zero !!!!-----
c
c-----
      integer m,le,r,rdim,mid,mdim
      integer groundup,groundlow

      real a,b
      real ky
      real h(20),epsr(20),mur(20),loss_tan(20),mu_tan(20)
      real mu0,eps0,pi,omega

      complex k(20),kx(20),kz
      complex j,k0,sum
      complex er_c(20),mur_c(20)
      complex zc(2,20),z0(2,0:21)
      complex twg,zs

      external twg
c-----
      common/constant/mu0,eps0,pi,omega,j,k0
      common/param/mdim,le
      common/mode/m
      common/mike/er_c,mur_c
      common/geometry/zs,groundup,groundlow
      common/geom/a,b
      common/layers/rdim,h,epsr,mur,loss_tan,mu_tan
      common/dimensions/mid

c-----
      ky = m * pi / b

      do 410 r=1,rdim

         k(r) = k0 * csqrt( er_c(r)*mur_c(r) )
         kx(r) = csqrt( k(r)**2 - ky**2 - kz**2)
         zc(1,r) = cmplx(omega * mu0 * mur_c(r)) / kx(r)
         zc(2,r) = kx(r) / cmplx(omega * eps0 * er_c(r))

      410 continue

c-----
      i = le

      z0(i,0) = zs * groundup
      z0(i,rdim+1) = -zs * groundlow

      do 420 r=1,mid
         z0(i,r) = zc(i,r) *
&              (z0(i,r-1)+j*zc(i,r)*twg(kx(r)*h(r)))/
&              (zc(i,r)+j*z0(i,r-1)*twg(kx(r)*h(r)))
      420 continue

      do 430 r=rdim,mid+1,-1
         z0(i,r) = zc(i,r) *
&              (z0(i,r+1)+j*zc(i,r)*twg(-kx(r)*h(r)))/

```

[illegible]

```

&      ' [EL10M]', ' [EL11M]', ' [EL12M]', ' [EL13M]', ' [EL14M]',
&      ' [EL15M]', ' [EL16M]', ' [EL17M]', ' [EL18M]', ' [EL19M]' /
data menu_mu/ ' [M1M]', ' [M2M]', ' [M3M]', ' [M4M]',
&      ' [M5M]', ' [M6M]', ' [M7M]', ' [M8M]', ' [M9M]',
&      ' [M10M]', ' [M11M]', ' [M12M]', ' [M13M]', ' [M14M]',
&      ' [M15M]', ' [M16M]', ' [M17M]', ' [M18M]', ' [M19M]' /
data menu_layer/ ' [L1B]', ' [L2B]', ' [L3B]', ' [L4B]',
&      ' [L5B]', ' [L6B]', ' [L7B]', ' [L8B]', ' [L9B]',
&      ' [L10B]', ' [L11B]', ' [L12B]', ' [L13B]', ' [L14B]',
&      ' [L15B]', ' [L16B]', ' [L17B]', ' [L18B]', ' [L19B]' /

```

\*\*\*\*\*

```

*      DEFINE WRITES A FILE CONTAINING ALL OF THE PARAMETERS NEEDED FOR
*      THE ANALYSIS OF THE INHOMOGENEOUSLY-FILLED WAVEGUIDE PROBLEM.
*      THE VARIABLES AND PARAMETERS ARE NAMED AS FOLLOWS:

```

```

*      a          - dimension of cavity along x axis
*      b          - dimension of cavity along y axis
*      fop        - frequency of analysis in GHz
*      fopstop    - maximum frequency
*      incrf      - frequency increment
*      rdim       - number of layers in cavity substrate

```

\*\*\*\*\*

```

C      THE NEXT SEGMENT DETERMINES WHETHER AN EXISTING CONFIGURATION FILE IS
C      TO BE USED

```

\*\*\*\*\*

```

100 write(*,*) 'Enter name of configuration data file; '
   read(*, '(A50)') config_file           {geometric configuration file name}
   cfg_file=config_file
   inquire(file=cfg_file, exist=exists) {check if format file already exist}
   call trim(cfg_file, 50, i1, i2)
   if (exists ) then
      warning = '   WARNING: File '//cfg_file(i1:i2)//
&      ' already exists. Use existing file?'//
&      ' ( <return> = yes )'
      write (6,*) warning
      read (5, '(a1)') ans
      if ((ans.ne.'y').and.(ans.ne.'Y').and.(ans.ne.'')) goto 100
      goto 200
   endif

```

\*\*\*\*\*

```

C      NEXT SECTION OF CODE IS ONLY REACHED IF NO CONFIGURATION FILE ALREADY
C      EXISTS AND WILL COLLECT ALL OF THE NECESSARY INPUT AND GENERATE A NEW
C      CONFIGURATION

```

\*\*\*\*\*

```

949 write(*,*) 'ENTER START FREQUENCY (GHz) : '
   read(*,*, err=949) fop
950 write(*,*) 'ENTER STOP FREQUENCY (GHz) : '
   read(*,*, err=949) fopstop
951 write(*,*) 'ENTER INCREMENT FREQUENCY (GHz): '
   read(*,*, err=949) incrf

   write(*,*) 'Select units: '
   write(*,*) '[1] inches '
   write(*,*) '[2] centimeters '
   read(*,*) lunit

```

```

write(*,*)
write(*,*) 'Enter # OF LAYERS IN WAVEGUIDE: '
read(*,*) rdim

x = 0.0
do i = 1, rdim

    write(*,*)
    write(*,*)
    &    'Enter permittivity for layer ',i
    read(*,*) epsr(i)
    if (epsr(i) .eq. 0.0) epsr(i) = 1.0
    write(*,*)
    &    'Enter permittivity loss tangent for layer ',i
    read(*,*) loss_tan(i)
    write(*,*)
    &    'Enter permeability for layer ',i
    read(*,*) mur(i)
    if (mur(i) .eq. 0.0) mur(i) = 1.0
    write(*,*)
    &    'Enter permeability loss tangent for layer ',i
    read(*,*) mu_tan(i)

    write(*,*) 'Enter height of layer ',i
    read(*,*) h(i)

    x = x + h(i)
enddo

```

```

*****

```

```

*    WAVEGUIDE GEOMETRY

```

```

*****

```

```

write(*,*) 'Enter waveguide dimension along x: '
read(*,*) a

write(*,*) 'Enter waveguide dimension along y: '
read(*,*) b

if (x .ne. a) then
    goto 499
endif

```

```

*****

```

```

*    NUMERICAL PARAMETERS

```

```

*****

```

```

write(*,*) 'Enter maximum # of modes to find'
read(*,*) mdim

do_gcl = .false.
do_ucl = .false.
le = 2
sig = 0.0

goto 400

```

```

C*****
*   THE NEXT SEGMENT READS DATA FROM EXISTING FILE
C*****

```

```

200 open(10,file=config_file)

```

```

    read (10,*)
    read (10,650) config_file
    read (10,*)
    read (10,*) mdim
    read (10,*)
    read (10,*) lunit
    read (10,*)
    read (10,*) a,b
    read (10,*)
    read (10,*) fop,fopstop,incrfr
    read (10,*)
    read (10,*) rdim
    read (10,*)
    do i = 1,rdim
        read(10,*) h(i),epsr(i),mur(i),loss_tan(i),mu_tan(i)
    enddo
    read (10,*)
    read (10,*) do_gcl
    read (10,*) do_ucl
    read (10,*)
    read (10,*) sig
    read (10,*)
    read (10,*)
650 format(A50)

    close(10)

```

```

*****
C   THE NEXT PART IS THE MAIN PART OF THE MENU SYSTEM
*****

```

```

*****
*   WRITE VARIABLE LIST ON SCREEN
*****

```

```

400 continue

```

```

    if (lunit.eq.2) then
        write(*,*) 'DIMENSIONS ARE TO BE ENTERED IN CENTIMETERS '
        un = 'CM'
    else if (lunit.eq.1) then
        write(*,*) 'DIMENSIONS ARE TO BE ENTERED IN INCHES '
        un = 'INCH'
    endif

```

```

    write(*,*)
    write(*,*) '*****'
    write(*,*)
    write(*,705) config_file
    write(*,*)
    write(*,704) un
    write(*,710) a

```

```

        write(*,715) b
        write(*,*)

704 format('the units are ',A7)
705 format('Name of geometry configuration file      [NAME] ', A50)
710 format('cavity dimension along x      [A]   : ',
& f14.7)
715 format('cavity dimension along y      [B]   : ',
& f14.7)

        write(*,*) 'START FREQUENCY TO RUN (GHz)  [FSTR]: ' ,fop
        write(*,*) 'STOP FREQUENCY TO RUN  (GHz)  [FSTP]: ' ,fopstop
        write(*,*) 'INCREMENT FREQUENCY      (GHz)  [FNCR]: ' ,incrfr
        write(*,*)

c 716 format('frequency',i3,' in GHz',3x,A7,2x,f14.7)

        write(*,*)
        write(*,*) 'NUMBER OF DIELECTRIC LAYERS      [NLY] : ',rdim
        if (rdim.gt.1) then
            write(*,*)
            write(*,*) 'RELATIVE ELECTRIC PARAMETERS OF LAYERS:'
            write(*,*) '                dielectric      ',
& '                loss                permeability'
            write(*,*) '                constant      ',
& '                tangent                real                ',
& '                imaginary'
            do i = 1,rdim
                write(*,720) i,menu_elr(i),epsr(i),menu_eli(i),
& loss_tan(i),menu_elm(i),mur(i),menu_mu(i),
& mu_tan(i)
            enddo

            write(*,*)
            write(*,718) un
            write(*,*) '
& ' -----'
            do i = 1,rdim
                write(*,725) i,menu_layer(i),h(i)
            enddo

            write(*,*)
        endif
718 format('GEOMETRY OF DIELECTRIC LAYERS:      ',2x,A7)
720 format('Layer',i3,5x,A7,' : ',f12.6,2x,A7,' : ',f12.6,
& 2x,A7,' : ',f12.6,2x,A7,' : ',f12.6)
725 format('Layer',i3,' thickness;      ',A7,' : ',f12.6)

        write(*,*)
        write(*,*) 'PROGRAM PARAMETERS '
        write(*,777) mdim
        write(*,*)
        write(*,*) 'CONDUCTOR LOSSES '
        write(*,744) do_gcl
        write(*,745) do_ucl
        write(*,746) sig

777 format('max. n mode number      [M] ', i5)
744 format('Include lower ground losses      : ',8x,' [GL] ',11,5x)

```



```
745 format('Include upper ground losses      :',8x,' [UL]  ',11,5x)
746 format('Conductivity of the walls        :',8x,' [SIG] ',e15.8)
```

```
C      goto 9999
```

```
*****
*****
*****
```

```
C      THE NEXT PART READS THE RESPONSES TO THE MENU PROMPT
C      DETECTS WHICH VARIABLE IS TO BE CHANGED
C      PROMPTS FOR THE CHANGE AND MAKES IT
C      AND UPDATES THE MENU
```

```
*****
```

```
write(*,*)
write(*,*) 'Enter Variable Name [**] or <return>'
```

```
read(*, '(A4)', err=499) check
```

```
***** ALTER VARIABLES AS DESIRED
```

```
if (check.eq.'') goto 600
```

```
if ( (check.eq.'STOP') .or. (check.eq.'stop')
&    .or.(check.eq.'QUIT') .or. (check.eq.'quit')
&    .or.(check.eq.'EXIT') .or. (check.eq.'exit')
&    .or.(check.eq.'ABORT') .or. (check.eq.'abort') ) stop
```

```
501 if ((check.eq.'name') .or. (check.eq.'NAME')) then
    write(*,*) 'ENTER NEW CONFIGURATION FILE NAME '
    read(*, '(a50)', err=499) name_file
    call trim(name_file, 50, i1, i2)
    inquire(file=name_file(i1:i2), exist=exists)
    if(exists) then
        warning = ' WARNING: File '//name_file(i1:i2)//
&                ' already exists. Input existing file? '//
&                ' ( <return> = yes ) '
        write (6,*) warning
        read (5, '(a1)') ans
        if ((ans.ne.'y') .and. (ans.ne.'Y') .and. (ans.ne.'')) goto 501
        config_file=name_file
        cfg_file=name_file
        goto 200
    else
        config_file=name_file
        cfg_file=name_file
        goto 400
    endif
endif
```

```
if ((check.eq.'a') .or. (check.eq.'A')) then
    write(*,*) 'ENTER A '
    read(*, *, err=499) a
    goto 400
endif
```

```
if ((check.eq.'b') .or. (check.eq.'B')) then
    write(*,*) 'ENTER B '
```

```
      read(*,*,err=499) b
      goto 40^
    endif

    if ((check.eq.'fstr').or.(check.eq.'FSTR')) then
      write(*,*) 'ENTER START FREQUENCY (in GHz)'
      read(*,*,err=499) fop
      goto 400
    endif

    if ((check.eq.'fstp').or.(check.eq.'FSTP')) then
      write(*,*) 'ENTER STOP FREQUENCY (in GHz)'
      read(*,*,err=499) topstop
      goto 400
    endif

    if ((check.eq.'fncr').or.(check.eq.'FNCR')) then
      write(*,*) 'ENTER FREQUENCY INCREMENT (in GHz)'
      read(*,*,err=499) incrfr
      goto 400
    endif

    if ((check.eq.'nly').or.(check.eq.'NLY')) then
      write(*,*) 'ENTER # OF DIELECTRIC LAYERS'
      read(*,*,err=499) rdim
      goto 400
    endif

    do i = 1, rdim
      if ((check(1:1).eq.'e').or.(check(1:1).eq.'E')) then
        if ((check(2:2).eq.'l').or.(check(2:2).eq.'L')) then
          if ((check(4:4).eq.'r').or.(check(4:4).eq.'R')) then
            if (check(3:3).eq.menu_elr(i)(4:4)) then
              write(*,*) 'ENTER ',menu_elr(i)
              read(*,*,err=499) epsr(i)
              eps(i) = epsr(i) * cmplx(1.,loss_tan(i))
              goto 400
            endif
          else if ((check(4:4).eq.'i').or.(check(4:4).eq.'I')) then
            if (check(3:3).eq.menu_eli(i)(4:4)) then
              write(*,*) 'ENTER ',menu_eli(i)
              read(*,*,err=499) loss_tan(i)
              eps(i) = epsr(i) * cmplx(1.,loss_tan(i))
              goto 400
            endif
          else if ((check(4:4).eq.'m').or.(check(4:4).eq.'M')) then
            if (check(3:3).eq.menu_elm(i)(4:4)) then
              write(*,*) 'ENTER ',menu_elm(i)
              read(*,*,err=499) mur(i)
              goto 400
            endif
          else if ((check(5:5).eq.'r').or.(check(5:5).eq.'R')) then
            if (check(4:4).eq.menu_elr(i)(5:5)) then
              write(*,*) 'ENTER ',menu_elr(i)
              read(*,*,err=499) epsr(i)
              eps(i) = epsr(i) * cmplx(1.,loss_tan(i))
              goto 400
            endif
          endif
        endif
      enddo
```

```
      else if ((check(5:5).eq.'i').or.(check(5:5).eq.'I')) then
        if (check(4:4).eq.menu_eli(i)(5:5)) then
          write(*,*) 'ENTER ',menu_eli(i)
          read(*,*,err=499) loss_tan(i)
          eps(i) = epsr(i) * cmplx(1.,loss_tan(i))
          goto 400
        endif
      else if ((check(5:5).eq.'m').or.(check(5:5).eq.'M')) then
        if (check(4:4).eq.menu_elm(i)(5:5)) then
          write(*,*) 'ENTER ',menu_elm(i)
          read(*,*,err=499) mur(i)
          goto 400
        endif
      endif
    endif
  endif
if ( (check(1:1).eq.'l').or.(check(1:1).eq.'L') ) then
  if ( (check(3:3).eq.'b').or.(check(3:3).eq.'B') ) then
    if ( check(2:2).eq.menu_layer(i)(3:3) ) then
      write(*,*) 'ENTER ',menu_layer(i)
      read(*,*,err=499) h(i)
      goto 400
    endif
  else if ((check(4:4).eq.'b').or.(check(4:4).eq.'B')) then
    if ( check(3:3).eq.menu_layer(i)(4:4) ) then
      write(*,*) 'ENTER ',menu_layer(i)
      read(*,*,err=499) h(i)
      goto 400
    endif
  endif
endif
if ( (check(1:1).eq.'m').or.(check(1:1).eq.'M') ) then
  if ( (check(3:3).eq.'m').or.(check(3:3).eq.'M') ) then
    if ( check(2:2).eq.menu_mu(i)(3:3) ) then
      write(*,*) 'ENTER ',menu_mu(i)
      read(*,*,err=499) mu_tan(i)
      goto 400
    endif
  else if ((check(4:4).eq.'m').or.(check(4:4).eq.'M')) then
    if ( check(3:3).eq.menu_mu(i)(4:4) ) then
      write(*,*) 'ENTER ',menu_mu(i)
      read(*,*,err=499) mu_tan(i)
      goto 400
    endif
  endif
endif
endif
enddo

if ((check.eq.'m').or.(check.eq.'M')) then
  write(*,*) 'ENTER M'
  read(*,*,err=499) mdim
  goto 400
endif

if ((check.eq.'gl').or.(check.eq.'GL')) then
  do_gcl = .not.do_gcl
  goto 400
endif
```

```
endif

if ((check.eq.'ul').or.(check.eq.'UL')) then
  do_ucl = .not.do_ucl
  goto 400
endif

if ((check.eq.'sig').or.(check.eq.'SIG')) then
  write(*,*) 'ENTER CONDUCTIVITY OF THE WALLS (S/m)'
  read(*,*,err=499) sig
  goto 400
endif

499 write(*,*)
write(*,*) '*****'
write(*,*) '          Entry format error -- try again          '
write(*,*) '*****'
write(*,*)
goto 400

*****
C   THE NEXT PART IS THE LAUNCHING POINT FOR THE REST OF THE PROGRAM
C   IT IS ONLY REACHED WHEN FINISHED WITH THE MENU PART
*****

*****

600 continue

*****
***** WRITE VARIABLES TO NEW FILE OR OLD FILE
500 call trim(cfg_file,50,i1,i2)
inquire(file=cfg_file,exist=exists)
if(exists) then
  write(*,*) 'File already exists --- ',
&           'overwrites not allowed.'
  write(*,*) 'Rename [R] or <return> (-- changes not saved)'
  read(*, '(A8)') ans
  if (ans.ne.'') then
    if (ans.ne.'override') then
      goto 501
    else
      goto 599
    endif
  endif
else
599  open(10,file=cfg_file,status='write')
    CALL WRITEOUT(10)
    close(10)
endif

*****

9999 return
end

*****
*****
```

```

.....
      subroutine trim(char_str,length_spec,i1,i2)
c.....c
c      finds positions of the first and last non-blank characters
c      in a string
c.....c
      integer length_spec,i1,i2,i
      character(*) char_str
      do 10 i=1,length_spec
        if (char_str(i:i).ne.' ') then
          i1=i
          goto 15
        endif
10      continue
15      do 20 i=length_spec,i,-1
        if (char_str(i:i).ne.' ') then
          i2=i
          goto 25
        endif
20      continue
25      return
      end

```

```

.....
*      SUBROUTINE WRITEOUT WRITES ALL OF THE PARAMETERS FOR THE PROBLEM IN
*      THE FILE OPENED AS file = ifile IN THE CALLING PROGRAM.
*
*      THE NORMALIZED PARAMETERS (a,b,c,...) ARE PASSED IN THE COMMON STATEMENT
*      AND WHEN WRITEOUT IS CALLED ARE ASSUMED NORMALIZED TO FREE SPACE WAVELENGTH
*      WRITE OUT RENORMALIZES TO WAVELENGTHS IN THE HOST MEDIA
*      BEFORE WRITING OUT TO THE DATA FILE.
*.....

```

```

SUBROUTINE WRITEOUT(ifile)

```

```

integer mdim,le,rdim,lunit
integer ifile,i,n

```

```

real a,b
real fop,fopstop,incrfr,unit,sig
real h(20),epsr(20),mur(20),loss_tan(20),mu_tan(20)

```

```

logical do_gol,do_ucl

```

```

character*50 config_file

```

```

common/param/mdim,le
common/geom/a,b
common/freq/fop,fopstop,incrfr
common/layers/rdim,h,epsr,mur,loss_tan,mu_tan
common/operate/do_gol,do_ucl,sig

```

```

common/files/config_file
common/units/lunit,unit

write (ifile,*) '*** input data file :'
write (ifile,*) config_file
write (ifile,*) '*** maximum mode number :'
write (ifile,*) mdim
write (ifile,*) '*** units (1=inch, 2=cm) :'
write (ifile,*) lunit
write (ifile,*) '*** x and y dimensions :'
write (ifile,*) a,b
write (ifile,*) '*** start,stop and incrmt frequencies in GHz :'
write (ifile,*) fop,fopstop,incrfr
write (ifile,*) '*** number of layers :'
write (ifile,*) rdim
write (ifile,*) '*** height, epsr, mur, loss_tan(epsr),'
s      , ' loss_tan(mur) :'
do i = 1,rdim
  write(ifile,*) h(i),epsr(i),mur(i),loss_tan(i),mu_tan(i)
enddo
write (ifile,*) '*** losses below and above walls :'
write (ifile,*) do_gcl
write (ifile,*) dc_lcl
write (ifile,*) '*** conductivity of walls :'
write (ifile,*) sig
write (ifile,*)
write (ifile,*)

return
end

```

-----  
SUBROUTINE LOGO

THE UNIVERSITY OF MICHIGAN COLLEGE OF ENGINEERING  
RADIATION LABORATORY  
ANN ARBOR, MICHIGAN

```

.....
.....
MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM
MM M  M MM  MM  MM  MM  MM  MM  MM  MM  MM  MM  MM  MM  MM
MM M M MM  MM  MM  MMMMMMMM  MM  MM  MM  MM  MM  M MM
MM M  MM  MM  MM  MM  MM  MM  MM  MM  MMMM  MMMMMMMMM  MM  M MM
MM  MM  MM  MM  MM  MM  MM  MM  MM  MM  MM  MM  MM  MMM
MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM  MMMM
.....
.....

```

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```

WRITE(*,*) ' '
WRITE(*,*) ' '
WRITE(*,*) ' '
WRITE(*,*) ' '
WRITE(*,*) ' '

```

```

WRITE(*,*) ' '
WRITE(*,*) '          THE UNIVERSITY OF MICHIGAN COLLEGE OF ENGI',
6 'NEERING'
WRITE(*,*) '          RADIATION LABORATORY'
WRITE(*,*) '          ANN ARBOR, MICHIGAN'
WRITE(*,*) ' '
WRITE(*,*) '*****',
6 '*****'
WRITE(*,*) '*****',
6 '*****'
WRITE(*,*) ' '
WRITE(*,*) 'MMMM      MMMM      MMMM      MMMM      MMMM      MMMM      MMMM      MMMM      ',
6 '      MMMM      MMMM      MMMM'
WRITE(*,*) ' MM M      M MM      MM      MM      MM      MM      MM      MM      MM      ',
6 '      MM      MM      MM      MM'
WRITE(*,*) ' MM M M MM      MM      MM      MMMMMMMM      MM      MM      ',
6 '      MM      MM      MM      M      MM'
WRITE(*,*) ' MM      M      MM      MM      MM      MM      MM      MM      MM      MMMM',
6 '      MMMMMMMM      MM      M      MM'
WRITE(*,*) ' MM      MM      MM      MM      MM      MM      MM      MM      MM      MM      ',
6 '      MM      MM      MM      MMM'
WRITE(*,*) 'MMMM      MMMM      MMMM      MMMM      MMMM      MMMM      MMMM      MMMM      ',
6 '      MMMM      MMMM      MMMM      MMM'
WRITE(*,*) ' '
WRITE(*,*) '*****',
6 '*****'
WRITE(*,*) '*****',
6 '*****'
WRITE(*,*) ' '
WRITE(*,*) 'THIS PROGRAM CALCULATES THE PROPAGATION CONSTANT ',
6 'OF THE HYBRID MODES'
WRITE(*,*) 'EXCITED IN PARTIALLY-FILLED WAVEGUIDES'
WRITE(*,*) ' '
WRITE(*,*) '      T. EMILIE  VAN DEVENTER  -- AND --  LINDA P. B.',
6 'KATEHI'
WRITE(*,*) ' '
WRITE(*,*) ' '
6 '      MARCH 11, 1990 VERSION'
WRITE(*,*) ' '
WRITE(*,*) ' '
WRITE(*,*) ' '
WRITE(*,*) ' '
PAUSE

RETURN
END

```

```

c*****
c
c          functions
c*****
c      complex function eqn_c(kz)
c
c      complex sum,fsum,kz
c      common/trick/fsum
c
c      sum = cmplx(0.,0.)
c      call hybrid(kz,sum)
c      eqn_c = sum

```

```
fsum=sum
```

```
return  
end
```

```
#####
```

```
complex function twg(arg)
```

```
complex arg,j
```

```
-----
```

```
i = cmplx(0.0,1.0)
```

```
if(aimag(arg) .gt. 45.0) then
```

```
    twg = j
```

```
else if (aimag(arg) .lt. -45.0) then
```

```
    twg = -j
```

```
else
```

```
    twg = csin(arg) / ccos(arg)
```

```
endif
```

```
return
```

```
end
```

```
#####
```



## References

- [1] R.F. Harrington, "Time-Harmonic Electromagnetic Fields", McGraw-Hill, 1961.
- [2] IMSL User's Manual, IMSL Library. Problem-Solving Software System For Mathematical and Statistical FORTRAN Programming, Edition 9.2, Revised November 1984, IMSL LIB-0009.
- [3] E. Yamashita, "Analysis of Microstrip-Like Transmission Lines by Nonuniform Discretization of Integral Equations," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-24, No. 4, pp.195-200, April 1976.